

# Analysis of the confirmation time in PoW blockchains

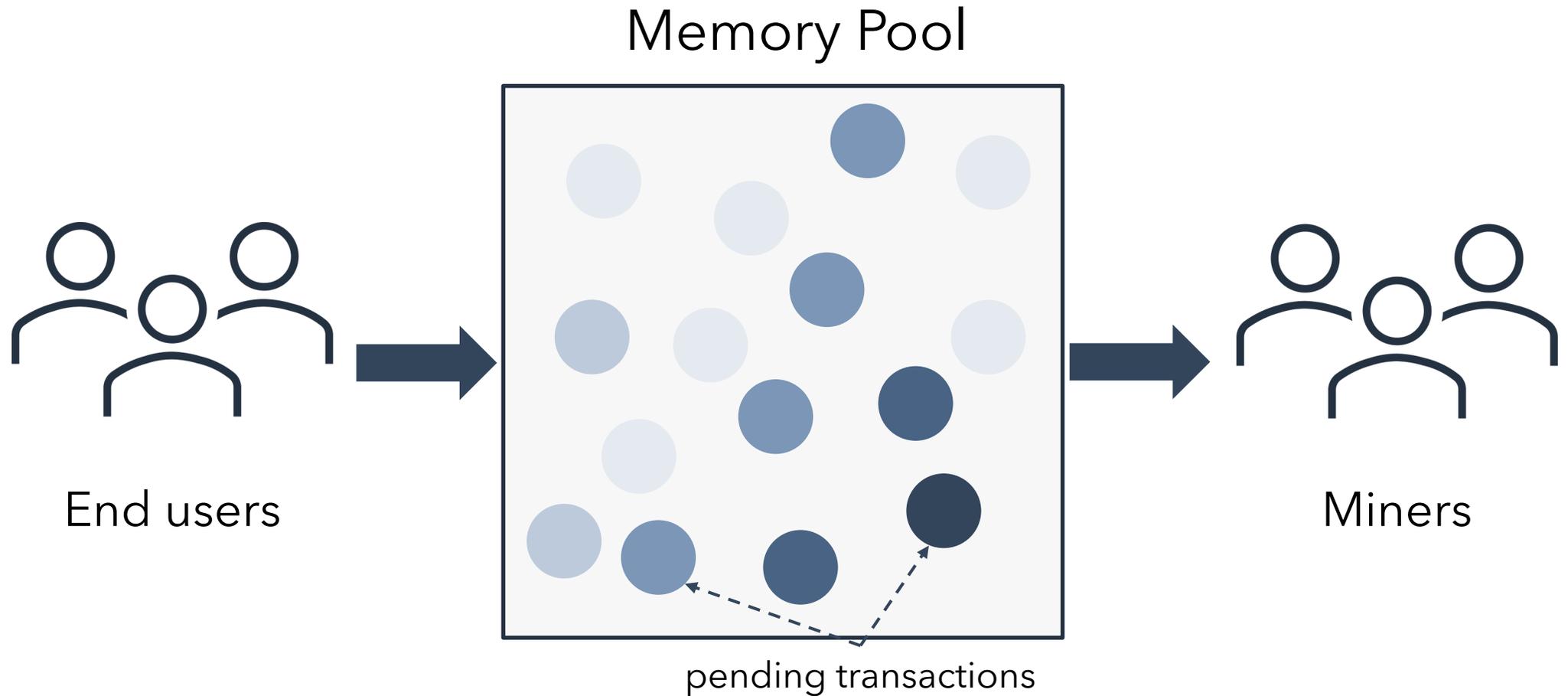
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# Context: Transaction flow

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# Context: Miner's incentive

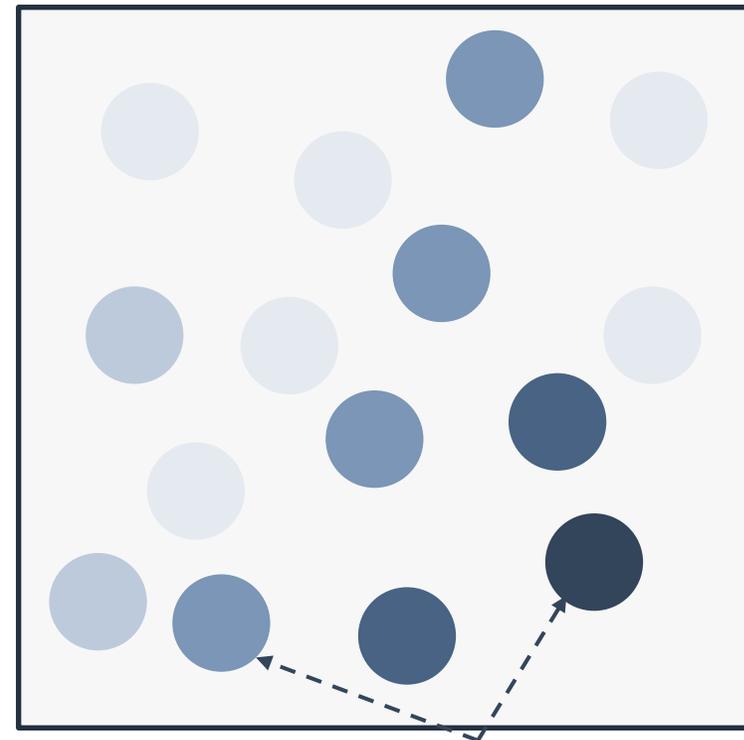
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Miner's reward is guaranteed:

- For each confirmed block
- For each transaction in this block

Miners select the transactions with highest fee\*

MemPool

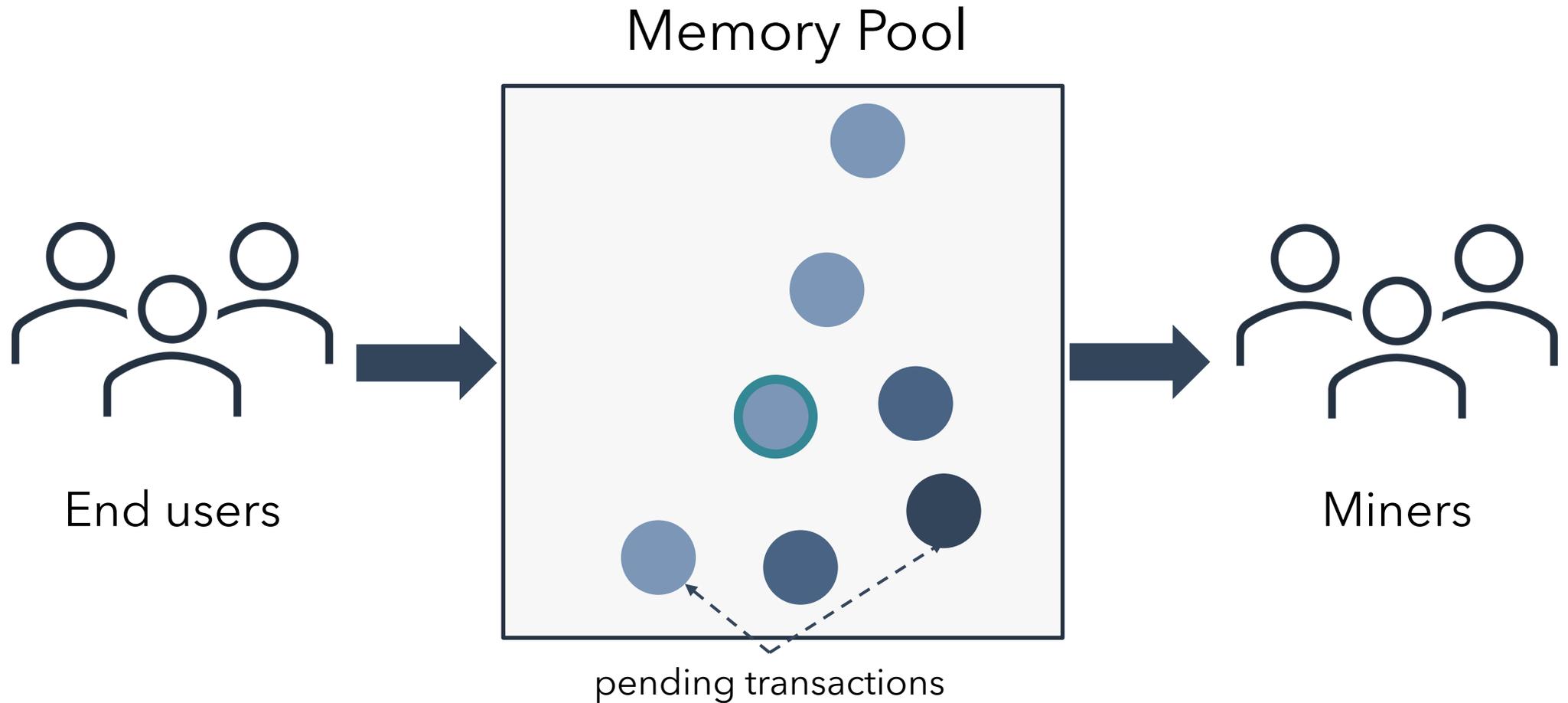


pending transactions

\* Fee per each byte of a transaction size

# Transaction flow

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# Context: Trade-off

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End users

Amount of transaction fee  
**VS**  
Transaction confirmation  
delay

# Problem statement

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*Investigate the relationship between offered fee and confirmation delay of transactions in PoW blockchain*

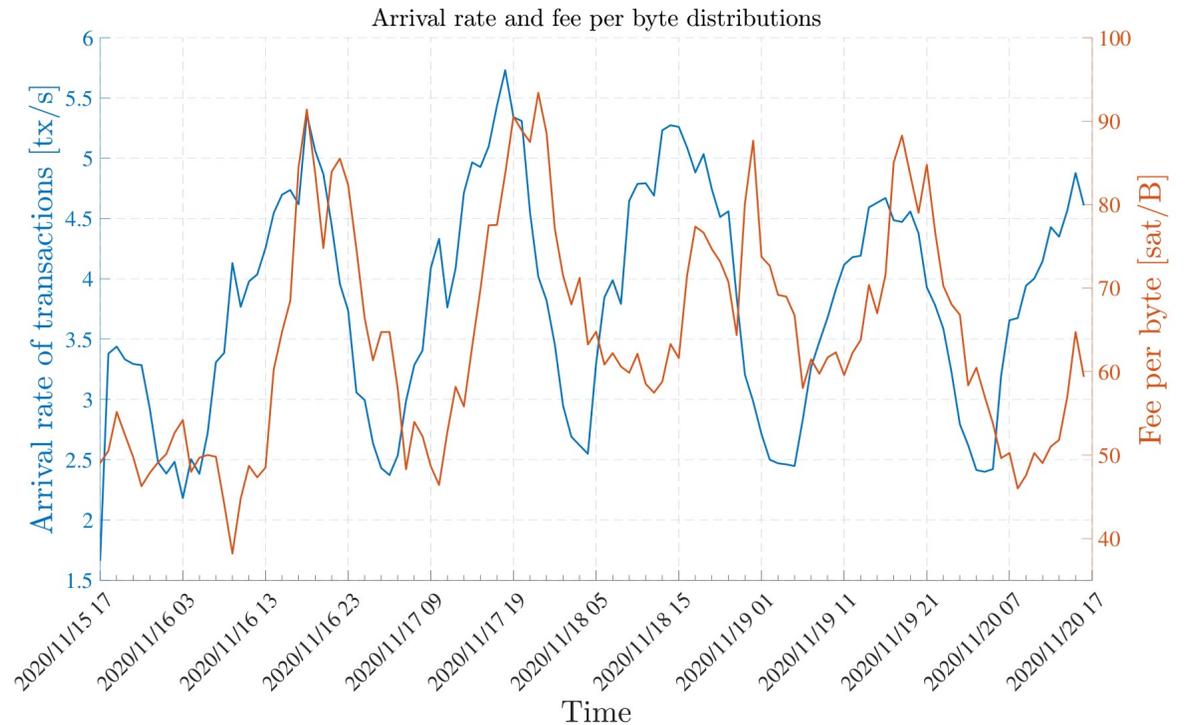
# State of the art

Fee determination methods:

Monte Carlo simulations

History-based approaches ('estimatesmartfee', BTC built-in function)

and others



Reactive nature of fee per byte and transaction arrival rate

# Analytical model

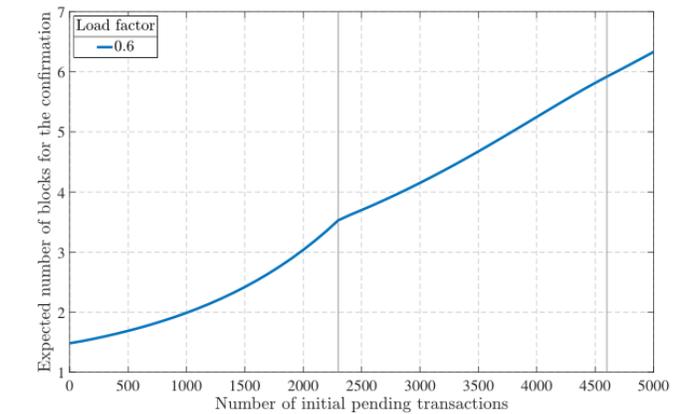
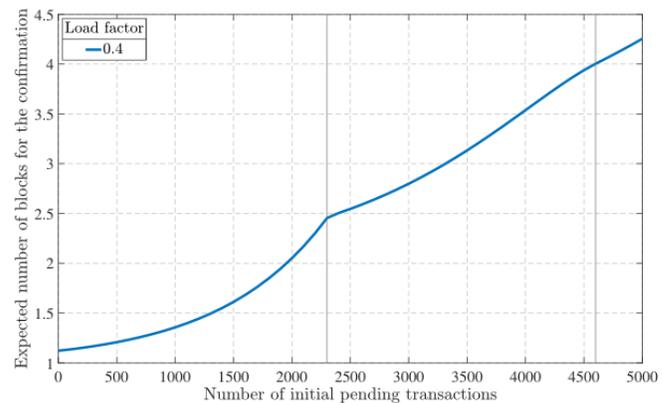
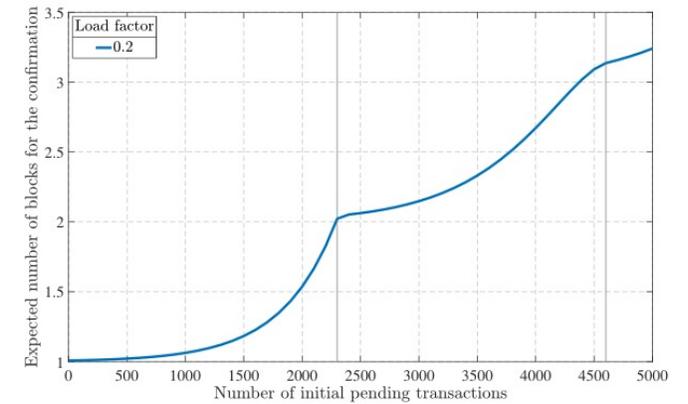
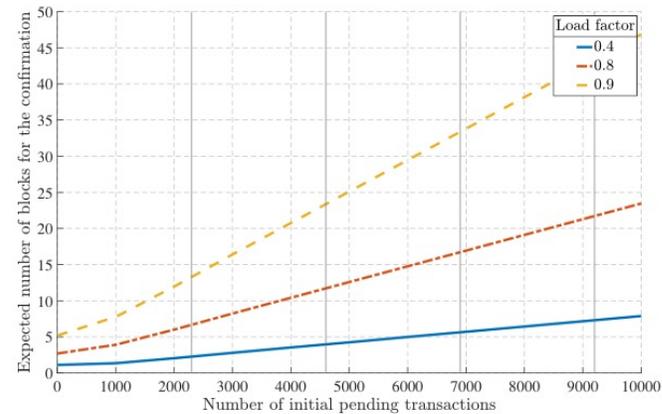
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M/M<sup>B</sup>/1 queueing system (B - batch/block size) considering:

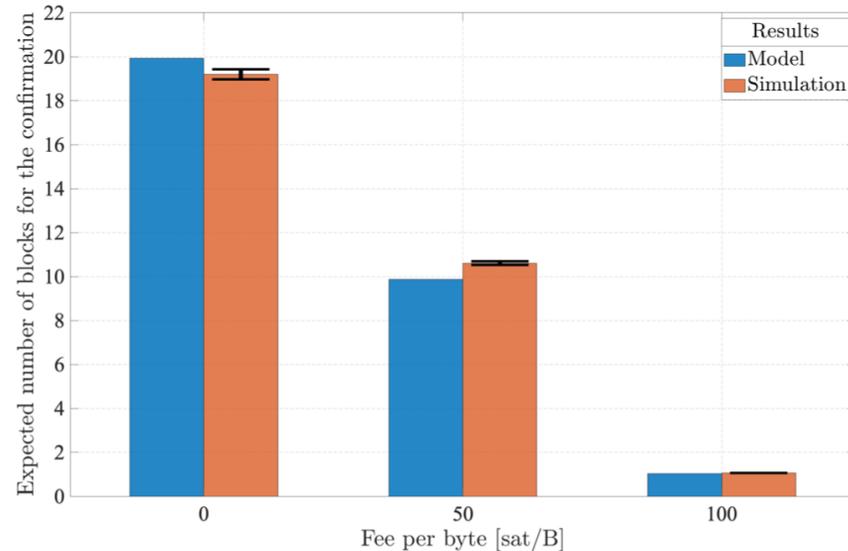
- Offered fee of target transaction
- Transaction arrival rate
- Mempool occupancy
- Fee distribution by other end users

# Numerical results

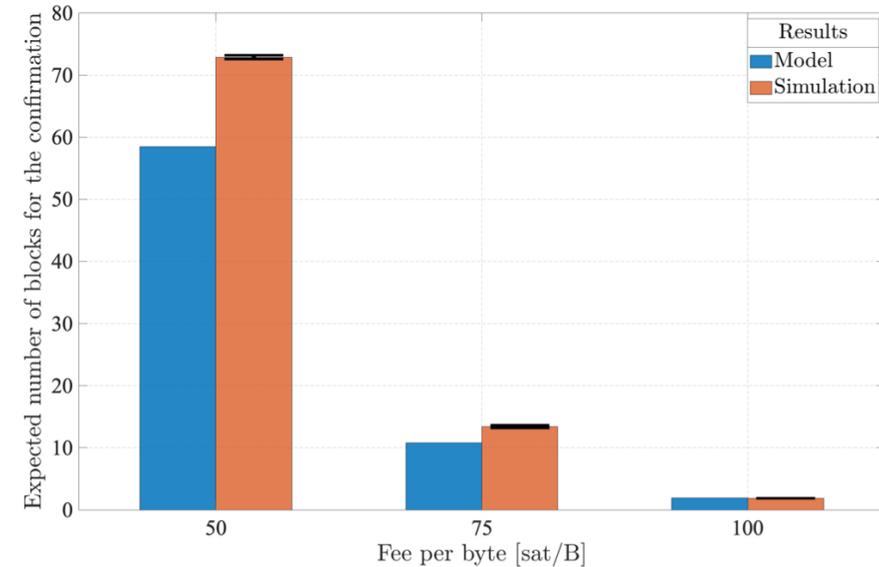
Impact of the initial Mempool occupancy on the expected confirmation time



# Validation: model VS simulation



Expected confirmation time (in blocks) as function of fee per byte for model and simulation results,  
 $Y=6,000$ ,  $\lambda = 3.21$  tx/s



Expected confirmation time (in blocks) as function of fee per byte for model and simulation results,  
 $Y=12,000$ ,  $\lambda = 4.02$  tx/s

# Conclusion

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- Introduction of  $M/M^B/1$  queueing model for confirmation time estimation based on:
  - Transaction offered fee
  - Mempool occupancy
  - Transaction fee distribution in Mempool
  - Transaction arrival rate

# Thank you!

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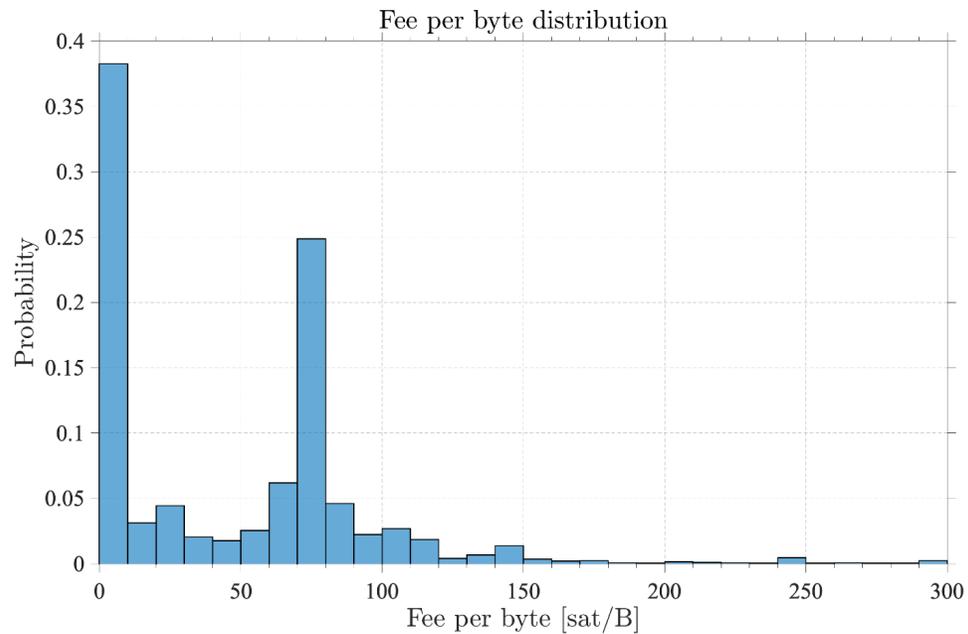
# Data

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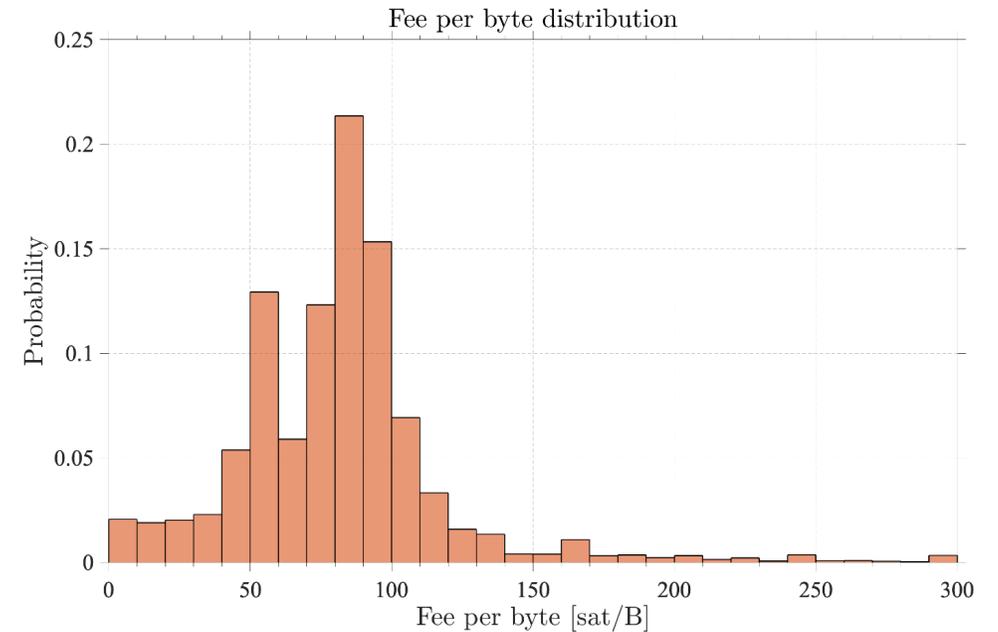
We have collected:

- over 1.5 million of pending TXs
- for 5 days (15/11/2020- 20/11/2020)

# Fee per byte distributions



Empirical probability density function  
in moderate workload conditions



Empirical probability density function  
in heavy workload conditions

# Main theorem

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- $M_1^Y$  - expected number of blocks for the transaction validation
- $Y$  - Mempool occupancy\* in transactions
- $P_1'(1)$  - constant determined with a numerical procedure
- $B$  - block occupancy
- $\alpha \triangleq \lambda / (\lambda + \mu)$  and
- $\beta \triangleq 1 - \alpha$

$$\begin{cases} M_1^1 = P_1'(1) \\ M_1^{Y+1} = M_1^Y + \frac{T_{Y-1}}{\alpha^{Y-1}} \left( M_1^1 + \frac{\beta}{\alpha} \right) - \frac{T_Y}{\alpha^Y} M_1^1, \end{cases}$$

where:

$$T_Y \triangleq \sum_{c=0}^{\lfloor \frac{Y}{B+1} \rfloor} (-1)^{c+1} \binom{Y - Bc}{c} \alpha^{Bc} \beta^c.$$

# Accuracy validation

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Empirical probability density function of relative error of actual and predicted confirmation delays.

